

1. (10 points) Solve the following differential equation.

$$(2x + \sin y) dx + (x \cos y + e^y) dy = 0$$

2. (10 points) Solve the following differential equation. Express your solution in *explicit form*.

$$y' = -\sin^2(x + y - 5)$$

3. (10 points) Solve the following initial-value problem. Express your solution in *explicit form*.

$$x y' + (x + 1) y = e^{-x} \ln x, \quad y(1) = 0$$

4. (10 points) Solve the following differential equation. Express your solution in *explicit form*.

$$x y' + x^2 y^3 = y$$

5. (6 points) Determine the region of the xy -plane for which the following differential equations possesses a unique solution. Explain your work and sketch the region.

a. $y' = \frac{y}{x}$

b. $y' = \sqrt{y-1} \sqrt{x}$

6. (10 points) Solve the following differential equation.

$$x^2 y' = y^2 e^{x/y} + xy$$

7. (9 points) The rate of change of a population of monkeys is proportional to the square root of the monkey population. Initially there are 100 monkeys and 2 years later there are 400 monkeys. How many monkeys will there be in 5 years?